# Numerations in the Sinhala Language

by Harsha Wijayawardhana edited by Aruni Goonetilleke



සිංහල භාෂාවේ සංඛාහංකනය හර්ෂ විජයවර්ධන සංස්කරණය - අරුණි ගුණතිලක පරිවර්තනය - එස්. එම්. බන්දුසීල

ICTA PUBLICATIONS

Numerations in the Sinhala Language

Author: Harsha Wijayawardhana Edited by Aruni Goonetilleke

#### Abstract

This paper covers the findings of recent research into archaic numerals in Sinhala language by the authors. Sinhala language in the present day uses numerals which were introduced by Portuguese, Dutch and English after 1505 AD and these numerals are known in Europe as Arabic numerals. The paper will also cover briefly of numerations and numerals existed in the recent past in Sinhala before 1815 AD of British occupation of Kandyan kingdom and it will also provide some of the findings of evolution of some of archaic Sinhala numerals into the form found at the time of British occupation of Kandy.

#### 1. Introduction

Sinhala belongs to the Indo-European Language family with its roots deeply associated with Indo-Aryan sub family to which the languages such as Persian and Hindi belong [Histroy1]. Although it is not very clear whether people in Sri Lanka spoke a dialect of Prakrit at the time of arrival of Buddhism in Sri Lanka, there is enough evidence that Sinhala evolved from mixing of Sanskrit, Magadi (the language which was spoken in Magada Province of India where Lord Buddha was born) and the local language which was spoken by people of Sri Lanka prior to the arrival of Vijaya in Sri Lanka, the founder of Sinhala Kingdom [Dissa06:11]. It is also surmised that Sinhala had evolved from ancient variant of Apabramsa (middle Indic) which is known as 'Elu'. Some scholars believe that 'Elu' is a type of Prakrit which was from India but others argue that it was native to Sri Lanka. When tracing history of Elu, it was preceded by Hela or Pali Sihala {Histroy1].

Sinhala though has close relationships with Indo Aryan languages which are spoken primarily in the north, north eastern and central India, and was very much influenced by Dravidian language families of South India especially by Tamil. Sinhala has borrowed many Tamil words which have become part of Sinhala vernacular. Though Sinhala is related closely to Indic languages, it also has its own unique characteristics: Sinhala has symbols for two vowels which are not found in any other Indic languages in India: 'Ae' ( $\alpha_{\chi}$ ) and 'Ae:' ( $\alpha_{\chi}$ ).

The Sinhala script had evolved from Southern Brahmi script from which all most all of the Southern Indic Scripts such as Telagu and Oriya had evolved. Later Sinhala was influenced by Grantha writing of Southern India. Since 1250 AD, the Sinhala script had remained the same with few changes. Although some scholars are of the view that Brahmi Script arrived with Buddhism, Mahavamsa (Great Chronicle) speaks of written language even right after the arrival of Vijaya. Archeologists had found pottery fragments in Anuradhapura Sri Lanka with old Brahmi script inscriptions, which had been carbon dated to 5<sup>th</sup> century BC. Earliest Brahmi Script found in India had been dated to 6<sup>th</sup> Century BC in Tamil Nadu though most of Brahmi writing found in India had been attributed to emperor Ashoka in the 3<sup>rd</sup> century BC[Brahmi02].

Sinhala letters are round-shaped and are written from left to right and they are the most circularshaped script found in the Indic scripts. The evolution of the script to the present shapes may have taken place due to writing on Ola leaves. Unlike chiseling on a rock, writing on palm leaves requires to be more round-shaped to avoid the stylus ripping the Palm leaf while writing on it. Drawing vertical or horizontal straight lines on Ola would have ripped the leaf and this also may have influenced Sinhala not to have a period or full stop, but instead a stylistic stop which was known as 'Kundaliya' was used. Period and commas were later introduced into Sinhala script after the introduction of paper due to the influence of the Western languages.

In modern Sinhala, Arabic numerals, which were introduced by Portuguese, Dutch and English are used for writing numbers and carrying out calculations. Roman numerals are used for writing dates and for listing items or words in Sinhala though at present, Roman numerals are not commonly used and they were also introduced by western powers who occupied Sri Lanka. It is accepted that Arabic numerals had evolved from Brahmi numerals. It had also been discovered by Sri Lankan archeologists that Brahmi numerals were used in ancient Sri Lanka and it may have evolved into a set of numerals which were known as archaic Sinhala numerals which were found in the Kandyan period. This paper will mainly cover archaic numerals and numerations in Sri Lanka at the time of British occupation of Kandyan Kingdom and their evolution to the forms which were found at the time of British occupation of whole of Sri Lanka. This paper will also touch upon Brahmi numerals, which was found in Sri Lanka.

#### 2. Approach and Methodology of research into Sinhala numerals

The authors carried out research into Sinhala numerals from the both linguistic and mathematical perspectives. In their research, the authors had looked specifically for the existence of zero in any form of numerations in Sinhala which were found in their research since the invention of zero had been a major demarcation point in mathematics and advancement in modern pure mathematics would have not been possible without having the concept of zero. Although zero had been discovered and rediscovered independently by various civilizations in the world, it is now accepted that zero as an independent number was discovered and used for the first time by the Indian mathematicians and it had been taken to the west by the Arabs with the rest of numerals which were developed in India from Brahmi numerals. E.T. Bell in his book, the development of Mathematics, describes of the development of zero by Indian mathematicians in the following manner:

"The problem of numeration was finally solved by Hindus at some controversial date before A.D. 800. The introduction of zero as a symbol denoting the absence of units or of certain powers of ten in a number represented by the Hindu numerals has been rated as one of the greatest practical inventions of all time"

[Bell40:51]

In their research into Sinhala numerals or numerations, the authors had looked into the following:

- i. Papers or publications on Sinhala numerals,
- ii. Original documents which had some of form of numerals or numerations,
- iii. Rock inscriptions,
- iv. Ola leaf page numbering,
- v. Any evidence for zero in Sinhala numerals or numerations,
- vi. Numismatics

Shapes of several numeral sets which belong to Indic languages were compared with of the numerals sets which were identified as numerals or numerations in Sinhala language. The Indic numerals sets which were studied extensively were Thai, Lao, Burmese, and Malayalam numerals.

The museums in Colombo and Kandy were visited many instances to study Ola leaf pagination by the authors. The Colombo museum library hosts an Ola leaf collection which is known as W. A. De Silva Collection and this sizable collection amounts to be 5000. Some of the original and older Ola leaf collections were found to be outside of Sri Lanka. A major collection is located in Britain and is known as Hugh Neville collection and the catalogue of this collection is available in Sri Lanka. Museums in other countries that are reputed to host Sinhala Ola leaf collections are in Arizona, US, Brussels, Belgium and Netherlands.

3. Numerals or numerations found immediately before the fall of Kandyan Kingdom

It had been found by the authors that five different types of numerations were used in Sinhala language at the time of occupation of Kandyan kingdom by the British. Out of the five types of numerations, two sets of numerations were in use in the twentieth century mainly for astrological calculations and to express traditional year and dates in ephemerides. The five types or sets of numerals or numerations are listed below.

i. Sinhala Numerals or Sinhala Illakkam

In "A Comprehensive Grammar of the Sinhalese Language", Abraham Mendis Gunasekera, the author of the book describes a set of archaic numerals which had not been in use even at the time of the publication of his book in 1891. According to Mr. Gunasekera, these numerals were used for ordinary calculations and to express simple numbers. These numerals had separate symbols for 10, 40, 50, 100, 1000[Guna1891:144]. These numerals were also regarded as Lith Lakunu or ephemeris numbers by W. A. De Silva in his "Catalogue of Palm leaf manuscripts in the library of Colombo Museum". This set of numerals was known as Sinhala illakkam or Sinhala archaic numerals.

The following is an excerpt from "A Comprehensive Grammar of Sinhalese Language", by Abraham Mendis Gunasekera describing Sinhala Archaic numerals:

"Sinhalese had symbols of its own to represent the different numerals which were in use until the beginning of the present century. Arabic Figures are now universally used" The old numerals are given in Figure 1 (No. iii.).

Plate III. 9 a Gn Cm Gm E A 1 2 3 5 6 C (CO) (CHG) Cala 8 10 9 7 11 12 Calon Calo Calan (CAIC) 13 14 15 16 B S Card (Calm) 6210 17 18 19 20 30 R BA (2/0) B 40 50 60 70 80 90 6 Gn 100 200 300 400 (0) 500 600 800 900 1000 Lith Surveyor General's Other Course NTEM

Figure 1: Archaic Sinhala Numerals from Plate III of Abraham Mendis Gunasekera's book 'A Comprehensive Grammar of Sinhalese Language'. These numerals did not have a zero and they also did not have zero concept holder.

an SY S 

Figure 2: Archaic numerals from 'Catalogue of Palm leaf manuscripts in the library of Colombo Museum', Volume I, compiled by W.A. De Silva, published by the Government Printer in 1938

One of the major findings had been the discovery of Sinhala numerals or Sinhala illakkam in the Kandyan convention which was signed between Kandyan chieftains and the British governor in 1815. Eleven clauses had been numbered in Arabic numerals in the English section of the agreement and the parallel Sinhala clauses were numbered in Sinhala Archaic numerals.

ලබරට නම්කුද 14 21/35 1815 held on the Star of March was on on Star and a star of the in the year of thand wis and mound an enough of wormowshe the Cingales year 17th not mode anone moust a war and an and the Balan in the City of Small Ger and Dowe Davadat 1000 Bar hours Between Harris mo Dow is Contenny Linder on many 600600 ස්මා Secret la chert Browning or 206 wide Des 200 Powerner and Commender Dos Son Son 200 in this in and ever the 2 horas horas and inde Buitish dellamateran Bach 3 2000 Desertence in the Aland Ing Good or Souse 5 of Puter reting in the Shi to good ant a basestario more and on behalled Die Die This Mapping George the Decorespondence thing thing, and des consorters Rougel History Color Color 5 Primer of Water Regard, siderstower enoughide of the united timoden & Swales Des and ad of Sund Abrilan and Son 500 Dog & cond 200 Parland in the Buer course of sologes part - min the station of 600000 Dessaves, and other 6 Chicks of යට 7

Figure 3: First page of the Kandyan Convention, 1815.

The handyou Cherines on goig a cover & some some wind be half of the Charles betand, I Soow Dean & Down a 6 and in presence of the asidewernouser ou Mohallales Cornals, 6-Nidaans and other Sub- 1 & Donores of comon 600 Derof ordinate Meadine from escologo of good at the deveral Provinces, DOGENGENSTO qe 200 and of the People their On EDD Dueser Dar we and and and the People the and the of the and the the other fart, it is again goon a so as a so and establishis as follows Syran 620000000 este 650 6600 1st That the Countlies and opportant of the made a seast and 30 ellalatar Rules, in the Dors Towns arbitrony and unfull mambre one influction of bodily 2656 Dordown 6 2000 Fortans and the pains or Dostan 6 100 3 Dears of death, witherst Chief some missed and and and Sometimes without Down porter owg main an accuration or the solder and papibility of a Crime; on mod coronon and in the general Con wormer ad sector of all binil Rights, have your so Devois De hecome flagraint, en - Orstede Der wow e

Figure 4: Second page with clear number one in Sinhala numerals

. . . . The Asto war morent of way 63000 ~ **~ ~ ~ ~ ~** Hallower ward having Bor equally and entirely Jan Dongan weren of that Planter which should decourse ຽ<del>ຊໄຣຍາ**ຊ**ີມາ ສອໂບ</del>ຊີຍ The its foles of His checkpels; Sect -දෙනෙක් න and of that good faith Down which winght colored an unus · longinal interent Star De de tom de a de with the mightening Decours elettermente. Alici er om 18 State Annual 20 Shal the Staffact sis son man dre M. Klenne Balah custo Ender Frences Janko, by the habitual son's Der Basis Dorder Micho line of the Charf Arman gon Barny ware & most Jacan Dutice & person رغيا ه دي ک of a clouringer, has for a zung more time files all Claund to Stad age in some same that Wille or the leven & exception is when mand to the strand, say 2 sisses berag 1 and in declara father Backasticky and defense from the Office of King Min the Samily and Arlating Sites 63 The he ther me the ascend of the former my deventing on a Francis copus, a so

Figure 5: 2 and 3 in Sinhala numerals in the Kandyan Convention



#### Figure 7: Sinhala archaic numerals with Sinhala numerals of Mendis Gunasekera.

The set of numerals found in the Kandyan convention has been given above with the numerals with Mendis Gunasekera's depiction of the same numerals .It is noteworthy to mention that number 2 and 3 of Sinhala numerals found in the Kandyan convention differ from the manner Mendis Gunasekera had depicted of the same set of numerals. The above set has been taken as the most accurate set when the shapes of the numerals are considered by the authors. The above assumption has been proven by examining the pocket watch of Sri Wickrama Rajasinghe, the last king of Kandy.

The watch gives considerable information as to how time was expressed in Sinhala. Sinhala day is made of Sixty Sinhala hours. Therefore the watch has thirty Sinhala hours for a half day.



Figure 8: the pocket watch of Sri Wickrama Rajasinghe the last king of Kandy.

The authors found an article in the Sinhala Encyclopedia on Sinhala numeration and numerals by Dr. P. D. S Kularatne former educationist and Principal of Ananda College of Sri Lanka who had given the shapes and description of the above numerals [Kula67]. In addition, the authors had found first Bible in Sinhala which was written at the time of the Dutch occupation where the year of compilation of the Bible was given using the above set.

#### ii. Lith Illakam or ephemeris numerals

Although this numeral set was commonly used for casting horoscopes and to carry out astrological calculations, the authors had found that this set had been used for numbering pages of Ola palm leaf books which covered primarily of non Buddhist topics. Dr. P. D. Kularatne in his article on Numerals and numerations in Sinhala language to Sinhala Encyclopedia claims that this set was used only for Astrological calculations [Kula67].



Figure 9: Number 1 in Lith Illakkam



Figure 10: Number 2

Banegeratiogerate TED OF HERE 370 2570 0,00000000 how 600 251262 ()II 38) ( 0530 6-3 m Pro CRE 070 1727 (Wall වහාන 2530

Figure 11: number 6 or akma

| Q.    | Number 1 or kombuwa                                |
|-------|--|
| 9     | Number 2 or letter Na from 8 <sup>th</sup> Century |
| al    | Number 3 or Naa from 8 <sup>th</sup> Century       |
| 6     | Number 4 or letter Ja                              |
| 9     | Number 5 or letter Da                              |
| ø     | Number 6 or Akma                                   |
| -1+   | Number 7 or letter OO                              |
| 50    | Number 8 or Letter Ra                              |
| 09    | Number 9 or letter Ni                              |
| A-    | Number 10 or Combination of Kombuwa and Halant     |
| 0696  | Number 11 or two kombuwas                          |
| and i | Number 13  |

Numbers of lith illakkam are depicted by Sinhala letters and vowel modifiers. The authors had discovered that there are mainly two versions of these illakam according to the way numbers 2, 3 and 9 are written. The number six is known as 'akma' in the Lith Illakkam. These numerals were in use continuously for writing horoscopes on Ola leaf, the tradition of which continued till the beginning of the twentieth century. Both versions of Lith illakkam have a zero and the zero is the Halantha or Hal lakuna (kodiya) in the Sinhala language. Although it is not understood whether Sinhala mathematicians treated zero as a number, it was quite possible they had known the concept of zero. In Lith Illakum, numbers greater than zero were written the same way as the Arabic numbers with the zero and the value of the number in the left was increased by ten. In other words, Lith Illakkam had a zero and a zero place holder concept. Lith Illakkam version 1 had for 2, 3 and 9, Sinhala letter 'Murthda Na' in 6 to 8<sup>th</sup> century. In the second version of Lith Illakkam as W. A. De Silva had depicted in his book, 2,3 and 9, Sinhala letter, 'Na' ( $\infty$ ) with vowel modifiers.



Figure 12: Lith illakkam version 1



Figure 13: second version of Lith Illakkam. W.A. De Silva describes Lith Illakkam; he had placed a vowel modifier for number 7 which has to be Letter OO

|            |          | ලිත් ඉලක        | ්කම     |              |
|------------|----------|-----------------|---------|--------------|
| 6          | හ        | හා              | ජ       | <del>ک</del> |
|            | 2        | 3               | 4       | 5            |
| 6          | Ĉ<br>7   | 6               | හි<br>ඉ | ର୍ଗ<br>10    |
| 66         | စော      | ອອງ             | රෙ      | ේද           |
| 11         | 12       | 13              | 14      | 15           |
| େ          | <u>ේ</u> | රෙ              | ଚ୍ଚ୍ଚେ  | ତ୍ରୌ         |
| 16         | 17       | 18              | 19      | 20           |
| <b>က</b> ေ | <b>ා</b> | <del>හ</del> නා | හජ      | <b>හද</b>    |
| 2၊         | 22       | 23              | 24      | 25           |

Figure 14: Dr. P. S. Kularatne on Lith Illakkam (20 is incorrectly depicted)

h

. . .

| මීළඟ<br>ඒවාද අ<br>ඒවා මේ | ට දැ<br>කුරු<br>මසේය | නගත<br>වෙයි. | යුත්<br>නුමුත් | තේ ලි<br>් ලිය2 | ත් ඉ.<br>න්නේ | ළක්ක<br>වමේ | ම් සම්<br>සිට ද | ම්බන්ධ<br>කුණට | )ව වෙ<br>ම වෙ | යි.<br>යි. |
|--------------------------|----------------------|--------------|----------------|-----------------|---------------|-------------|-----------------|----------------|---------------|------------|
| 1                        | 2                    | 3            | 4              | 5               | 6             | 7           | 8               | 9              | 10            |            |
| G                        | න                    | නා           | S              | ę               | ଜ             | c           | 0               | නි             | GJ            |            |
| naced a                  | and                  | -            | ana al         | 0 0             |               | - 10        | 0               | p p            |               |            |

Figure 15: (ලක් අංක) or Ephemeris numbers from Hendirk De Silva Hettigoda's Astrology book

Figure 15 provides third version of Lith Illakkam but the authors had not observed this version in general except in this particular book. The difference of this version is the zero, instead of hal lakuna, this version has a 'Pilla' with hal lakuna[Hetti87].

One of the most interesting articles which the authors had come across is an article on numerals and numerations in Sinhala language, by Abraham Mendis Gunasekera. In this article, he refers to Lith Illakum as well as to Sinhala Illakkam. For Sinhala Illakkam, he produces the same shapes which had been given in his book written in English. Abraham Mendis Gunasekera uses modern Sinhala letters and vowel modifiers which is Version 2 of Lith Illakkam. In this article, he clearly mentions that Hal lakuna or 'Kodiya' is the zero. In other words, 'Sunayathana' is filled with a kodiya will multiply by ten, the number on the left side of Sunayasthana. Abrham Mendis Gunasekera clearly states that instead of Hal lakuna of Sinhala language, a 'Shunaya binduawa' (zero place holder) can be used to fill the 'Shunayasthana'. In other words, Lith Illakkam uses duality of zero to write numbers greater than 9[Guna-Article1891]. This article counters that lith illakum may have been used up to 60 by P. D. S Kularatne[Kula67].

| ්ළිඛඳ ගණෑ<br>්වා මෙතේය   | න් කීමය<br>:  | ) ගාමනාකා | ই-হ্ছ ি    | (ତ୍ରର | <del>.</del> 5 |
|--|---|-----------|------------|-------|----------------|
|  | r.  |           | <i>6</i> 0 | මාණ   |                |
| Gerwys.  |   | ගම,       | අරාබ       | g Da  | 0 c3,          |
| $z_{ijj}^{T}$  | 62  | ාමබූව     |            | 1     |                |
| 1547733<br>North 200   | 20  | ගත්ත      |            | 2     |                |
| <i>3</i> 33a   | (75   | ායන්න     |            | 3     |                |
| terit.   | S   | යන්න      |            | 4     |                |
| 5 <sup>27</sup><br>3.  | 4 <u>7</u> C  | 0 ප් පා   |            | 5     |                |
| 63   | The second se | 25I D     |            | 6     |                |
| in the second se | ( <sup>**</sup> )(  | නත් හ     |            | 7     | (11)<br>(11)   |
| C.   | do  | නත් ක     |            | 8     |                |
|  | 855   | ත්හියන්න  |            | 9     |                |

ම ඉලකකාමවලට අල් ලකුණ හෙදුකල එහි විධිනාකම දශවාරයක් වැඩේ. එබැවින් ේ \* යනු 10 සි; න් යනු 20යි; න් යනු 80යි; මේආද මෙනි. ශූකකස කීමට බන්දුව (0) ද යොදත්. ගණන් දක්වීමට මේ ඉලක්කම්වල සෙදීම අරාබ ඉලක් කම ඉයාදන පිළිවෙලට වේ : එනම 84 යනු රජ; 102 යනු 6 \* නමක් ගෙන; 1547යනු දෙජල; 1807 යනු රෙහිල.

Figure 16: Abraham Mendis Gunasekera on Lith Illakkam. In his examples, he had used zero to write 102 instead hal lakuna

According to the above article, the following combinations given in figure 17 are possibilities.

According Abrham Mendis Ganesekens The folloing combinations are a possibility. 6000 or APO 102 102 alon also GOD - elamed by 102 102 102 AMG in h. article attert - of ott ? ott ? otto? ? numbers with question marks have . not been by the authors

Figure 17: possible combinations using lith Illakkam

Figure 18: Ephemeris found in the Kandy Museum



Figure 19: Degrees that Planets were positioned in Nakshathra



# Figure 20: Horoscope cast in October 1936



Figure 21: Same Horoscope with Lith Illakkam

The authors have found a horoscope which had been casted in 1932 in Matale using the same Lith Illakkam which has been included.

#### iii. Katapayadia

Even to this day, years are given in the front page of popular ephemeris in Sri Lanka, 'Panchanga Lith' using 'Katapayadia'. Katapayadia is a unique numbering scheme where numbers 1 to 9 and 0 have been depicted by consonants. The katapayadia is mainly used for writing dates.

| 1  | 2 | 3 | 4  | 5  | 6 | 7 | 8  | 9   | 0  |  |
|----|---|---|----|----|---|---|----|-----|----|--|
| ක  | ඛ | ග | ක් | ඞ  | Ð | 6 | 8  | 202 | şa |  |
| Ø  | ය | ඞ | ස  | Sn | ත | 0 | ę  | 0   | 20 |  |
| 0  | B | බ | භ  | ۲  |   |   |    |     |    |  |
| ය. | 0 | C | ව  | 3  | 8 | ස | 63 | 0   |    |  |

Figure 22: Katapayadia (borrowed from Life and Planets, the book written by Hedrick De Silva Hettigoda).

This is numeration is known as Katapayadia:<sup>1</sup> so called since number one is assigned the Sinhala letters 'Ka' ( $\varpi$ ), 'Ta' ( $\Im$ ), 'Pa' ( $\varpi$ ) and 'Ya' ( $\omega$ ). In this tradition of writing numbers, the year 2007 can be written with for instance 'Ka' ( $\Im$ ) 'Na' ( $\varpi$ ) 'Na' ( $\varpi$ ) 'Sa' ( $\varpi$ ). Traditionally, 2007 will be written from right to left: 7002. Ordinarily, using vowel modifiers, a word in Sanskrit will be created for the year 2007 (7002 right to left) with the allocated letters for 7002. When reading, one has to remove the vowel modifier.

Katapayadia was widely used by South Indian astrologers and some of Chola rock inscriptions in Sri Lanka have dates inscribed in Katapyadia.

## iv. Page numbering of Ola leaves using Sinhala 'Swara (ස්වර)'

The method of page numbering of Ola using Sinhala Swara had been common tradition in the ancient and recent history of Sri Lanka. The author had found that using Sinhala Swara in place of numeration could be traced back to Aryabhata's (the great Indian Mathematician and Astronomer) numbering system where he used Sanskrit Swaras in place of numerals. Sinhala scribes had developed their own numeration based upon Sinhala characters according to the order of the position of consonants and vowels in the Sinhala Alphabet without the modern two vowels: 'Ae' ( $q_{\tilde{\tau}}$ ) and 'Ae:' ( $q_{\tilde{\tau}}$ ) in the Sinhala Alphabet (the Sinhala alphabet without the above mentioned two vowels is known as 'Pansal Hodiya' or the alphabet of the temple). The numeration method which is similar to the use of Sinhala Swara is found in Burmese Ola collection.

The tradition of Swara as numeration in page numbering in Ola had been commonly used for Buddhist manuscripts. The authors had the opportunity of examining several Ola palm leaf books in the Colombo museum<sup>1</sup> and the catalogues of Hugh Neville<sup>5</sup> collection in the London Museum<sup>2</sup>. Having investigated paging of Ola leaves, the majority of palm leaf manuscripts which are in the museum had Sinhala consonants with 'swara' (cdOd) (combinations of sounds) for numbering. The number of combinations which can be made out of consonants is 544 and once the first 544 ends, paging begins with the second cycle of 544 with the word 'dwi:' (cdOd) or 'second' in English. If the second cycle does not end the palm leaf book, it goes into third cycle of 544 which begins with the word 'three' (cdOd) or Three in English [DeSilva38].

### v. Bhootha Anka or Butha Samkaya

In Sinhala literature, certain words in the language were used to denote numbers. For instance, sky is associated with zero or 'Sunaya', and a number which was denoted by words is known as Bhuta Anka. Bhootha Anka was created by ancient Sanskrit Mathematicians and Astronomer prior to the invention of a symbol for zero. Some of the words which are associated with numbers are

Moon = one

Eye = two

Fire = three

If one were to write 130, he or she would place moon, fire, sky together to form the number. Pierre-Sylvain Filliozat in his article 'Ancient Sanskrit Mathematics: an oral tradition and a written literature', describes Bhootha Anka as object-number metronomic expressions.

As it was mentioned previously, knowledge was transferred through memory rather than writing it down. In order to make memorization easier, it is natural that the numbers are placed as words and the words are formulated sequentially that they would sound rhythmical. The Indian tradition of Bhootha anka was imported to Sri Lanka as it was used in India and the tradition continued with Sinahala words that had same meanings.

#### 4. Brahmi numerals found in Sri Lanka

Dr. Senarath Paranavithana (first Sri Lankan Commissioner of Archaeology) and Prof. Abaya Aryasinha of the University of Kelaniya, had independently found in their research that Sinhalese had used numerals which closely resembled Brahmi numerals of India in the early days of Sinhala civilization. The evidence for use of Brahmi numerals had been discovered primarily in rock inscriptions which were inscribed in between AD 200 and 400. These numerals were used to record donations given by royals and other people who were belonged to the upper echelon of ancient Sinhala society to Buddhist temples [Abi90:90].

Brahmi numerals are ancestors of Arabic numerals which are used presently worldwide. Brahmi numerals had symbols for 10,100, and 1000. Number 1 and 10 in Brahmi have not been found in Sri Lanka up to now. Therefore shapes of these two numerals have been hypothesized without physical evidence [Menninger92:395]

Sinhala rock inscriptions suddenly become barren of numerals from A.D. 400 onwards. Tradition of writing numbers in word becomes more prevalent from the above period.

|   |   | 1        | 2        | 3       | 4       | 5       | 6      | . 7    | 8       | 3 5                | ) 1      | 0       |         |         |             |         |           |          |             |
|---|---|----------|----------|---------|---------|---------|--------|--------|---------|--------------------|----------|---------|---------|---------|-------------|---------|-----------|----------|-------------|
|   |   | -        | _        | Ξ       | +       | h       | . 6    | 5      | ) レ     | 5 (                | C        | X       |         |         |             |         | Ē         |          |             |
|   | 1 | 2        | 3<br>=   | 4<br>¥  | 5<br>[> | 6<br>Ge | 7<br>7 | 8<br>5 | פ<br>ר  | 10<br>X            | 20<br>29 | 30<br>ア | 40<br>又 | 50<br>J | 60 7<br>1 X | '0<br>( | 80<br>D ( | 90<br>Ð  | 100<br>ツ    |
| 1 | 2 | 3<br>. = | 4<br>: ¥ | 5<br>'h | 6<br>G  | 7<br>フ  | 8<br>S | 9<br>2 | 10<br>Y | <sup>20</sup><br>ඊ | 30<br>-  | 40      | 50<br>J | 60<br>- | 70<br>لا    | 80<br>- | 90<br>-   | 100<br>7 | ) 1000<br>J |

Figure 23: The first set was found during 3BC and the second was commonly found in 1AD in India and the Sri Lanka set is without 80 and 90



Figure 24: number 4 in the Kandy museum

? (10) (20) 2) (30) (3 40 (2 (5)/ 9 (50) E 60 (6) 70) 80 (8) / V 90 2 (9) 100] [J (10) ? / 10001

අංක 2 දරන රූප සටහනෙන් උපුටාගත් බුාහ්මී අංකන කුමය

4 වන රූප සටහන

Figure 25 Brahmi numerals in Sri Lanka[Abi90:90]

#### 5. Evolution of Sinhala Illakkam and Lith Illakkam

#### i. Sinhala Illakkam

Sinhala Illakkam had evolved from Brahmi numerals which were found in Sri Lanka. Since Brahmi number 1 and 10 had not been discovered in Sri Lanka, it is not possible to know the shapes of those two numerals in order to compare with Sinhala Illakkam. The shapes of these two numerals were surmised comparing with the Indian Brahmi numerals at the same period. In Sri Lanka Brahmi 4 had evolved parallel with the Indian Brahmi, but Sinhala Illakkam had evolved into more complex shapes than that of its Indian cousins (Arabic numerals had evolved from sets of Indian numerals) due to cursive shapes of Sinhala letters. Shapes of Brahmi number 100 and 1000 found in Sri Lanka are different from of Brahimi 100 and 1000 which are commonly found in India. The following is possible evolution of process of Brahmi into Sinhala Illakkam.



#### Figure 26 Evolution of Sinhala Illakkam

The authors modeled the evolution of Sinhala Illakkam using Morphing Software and modeling enables the authors to see possible stages of evolution we had not discovered physically. It can be quite easily seen the evolution of Numbers 1, 2 and 3 of Brahmi into Sinhala Illakkam comparing how Inidan numerals had evolved from the Indian Brahmi.

The authors have found some evidence for Sinhala Illakkam at the Wata Da Ge in Pollonaruwa. Floor tiles of Wata Da Ge at Pollonaruwa were made from rock slabs which were quarried and were brought from a far distance from the present location. Since Wata Da Ge is a circular structure, the builders had numbered the tiles before transporting them to the present location. At the Wata Da Ge, the researchers had found three different categories of numbering systems. At the first level, rock slabs were numbered using Sinhala 'Swara' and second level, clear number 1 of Sinhala Illakkam was found.



Figure 27: Sinhala Swara KU on the ground floor of Wata Da Ge in Polonnaruwa.



Figure 28: Sinhala Illakkam number 1

The three categories of numbering found at Wata Da Ge were

- 1. Possible Sinhala Illakkam
- 2. Swara based Numbering which was found in the Ola lead paging
- 3. Sanskrit letter (swara) and Indian Numeral

Figure 27 provides evidence for category 1 of numbering and figure 28 is a clear indication that some of Sinhala Illakkam had been used for numbering of rock tiles. The following is the evidence for third category of numbering at Wata Da Ge. When looking at the history of Wata Da Ge, it was originally built by King Parakramabahu the first and it was again restored by Nissanka Malla. At the end of Polonnaruwa period, Wata Da Ge had been destroyed and it was again restored for the last time during the Dambadeniya period in the ancient times until the 20<sup>th</sup> century.



Figure 29: Deva nagri Itha and suspected 7

#### 2. Evolution of Lith Illakkam or Ephemeris numbers

Unlike Sinhala Illakkam, the authors had a difficulty in tracing the evolution of Lith Illakkam. The authors had looked for any evidence in India for the origins of this set in vain. At present, almost all evidence points to very Sri Lankan origins of Lith Illakkam. Shapes of number 2, 3 and 9 of first version of Lith Illakkam are self evident. When their evolution is considered and it goes back to eighth and ninth century Sinhala Letter 'Murthda Na'. Therefore it can be surmised that the origins of this set would have been in the 8<sup>th</sup> and 9<sup>th</sup> century in Sri Lanka. The very selection of specific letters for 1 to 9 had been a puzzle for the authors from the inception of the research. The authors surmise at present, the selection of these letters had been based upon specific sounds and these sounds may have been allocated for specific nakshatra or nakath. There are 27 or 28 Nakshatra in the Indian zodiac and each Nakshatra has been allocated specific sounds. Though each letter and vowel modifier depicts a number in this set, in order to hear the sound, they have to be read together aloud. For instance number 1 and number 2 are depicted with 'Kombuwa' and letter 'Na' and they have to be sounded together. And number 5 is letter 'Da' and number 6 is 'ackma' which is a vowel modifier which is placed on top of a consonant. In this instance, one could sound these two together as 'Di'. What surprised the authors had been the beginning sound 'Ne' is fourth 'pada' and the end sound of 'Ni' is the first 'pada of Nakshatra Anurudha or Anuradha and the others sounds are placed sequentially one after another according to Nakshatras, completing a full circle.

The authors were further surprised in the manner that the zero had been depicted in the lith Illakkam. Hal lakuna or Halantha is a nullifier of a natural vowel sound in a consonant in Sinhala. Halathna in this aspect is a nullifier and since Sinhala letter had been used for writing numbers, whoever invented this set naturally used Hallantha or Hal Lakuna for the zero. In Sinhala, there are two ways that halantha can be used. Certain letter such as 'Ma', halantha is attached to the top of the letter without standard 'Kodia'. Kodia is the only halantha which has been used for the depiction of zero. Unlike other version of Halantha, kodia can be placed without a letter, and hence the authors surmise that large numbers with many zeros could have been written using 'kodia'.

#### 6. Conclusion

Although there is a vacuum and silence when Sinhala mathematics is concerned, it can be said without doubt that Sinhala language had several well developed numeral sets. Although numbers are depicted in words in many rock inscriptions after 400AD, the evolution of numerals may have occurred in parallel with the Sinhala letters from Brahmi numerals. Sinhala Illakkam is the older brother or sister of Arabic, and Devangri numerals. But unlike Arabic and Devanagri, it never evolved into a set with a zero. Instead Sinhala astrological mathematicians, or 'Ganithas', developed their own numerals set which is known as Lith Illakkam which was unique to Sri Lanka and it was based upon Sinhala consonants and vowel modifiers according to sound. This set possessed a clear zero and a zero place holder unlike Sinhala Illakkam. This numeral set was used to carry out tedious calculations such as finding exact timing of the end and the beginning of year based upon traversing of sun in the zodiac or movement of earth in the solar system. Further research is required to be carried out to establish whether Sinhala mathematicians had treated zero as a number.

#### References

[Bell40] Bell E.T. Development of Mathematics, Second Edition, , Mc-Grew Hill Book Company, Published 1940, 1945, page 51

[DeSilva38] De Silva W.A., from 'Catalogue of Palm leaf manuscripts in the library of Colombo Museum', Volume I, Government Printer, 1938

[Dissa06] Dissanayaka J. B., Sinahala Graphology, Sumitha Publication, 2006

[Epa07] Epa Panchanga (Epa Ephemeris), Epa Printers, 2007

[Ever07] Everson Michael, ISO/IEC JTC1/SC2/WG2 N3195R, Proposal to add archaic numbers for Sinhala to the BMP of UCS, 2007

[Filliozat04] Filliozat Pierre-Sylvain, Ancient Sanskrit Mathematics: an oral tradition and a written literature, this article is in the book 147, History of Science, History Text by Karine Chemla, 2004

[Guna1891] Gunasekera, Abraham Mendis A Comprehensive Grammar of Sinhalese Language, Sri Lanka Sahitya Mandalaya (Academy of Letters, 144-150, 1891.

[Hetti87] Hettigoda, Hendrick De Silva, Life and Planets, Vishwa Lekha, Sarvodaya, 34 -36, 1987 (First print in 1967)

[Indian98] Indian Epigraphy: A Guide to the Study of Inscriptions in Sanskrit, Prakrit, and the Other Indo-Aryan Languages, By Richard Salomon, Published by Oxford University Press US, 1998

[Jouv95] Jouveau-Dubreuil G., The Pallavas, V. S. Swaminadha Dikshita, Published by Asian Educational Services, 1995

[Kula67] Kularathne P.D.S, Article on Numeration, Sinhala Encyclopedia, 1967

[Masica93] Masica, Colin P., Indo Aryan Languages, Cambridge language surveys, 1993

[Menninger92]Menninger Karl, Paul Broneer Number words and number symbols: a cultural history of Translated by Paul BroneerPublished by Courier Dover Publications, 1992.

[Sam00] Samaranayake V. K., Nandasara S. T., Disanyake J.B., Weerasinghe A. R., Wijayawardhana, An Introduction to UNCODE for Sinala characters, H., 2000

[Mahanama03] Mahanama Thera, The Mahavamsa, The Great Chronical of Sri Lanka, Vijith Yapa publication 2003

[Abi90]අභිලේඛන, සමරු පොක් පෙළ, දෙවන වෙළුම, පුධාන සංස්කාරක - පණ්ඩික ආචාර්ය නන්දදේව විජේසේකර, පුරාවිදාාා දෙපාර්තමේන්තුව, 1990

[Guna-Article]1891]ගුණසේකර ඒබුැහැම් මෙන්දිස් ගුණ්ථාන්වය, කතෘ - (පිටු අංක 3 සිට 10 දක්වා)

[History1]History of Sinhala Language, accessed 29<sup>th</sup> of May 2009 http://en.wikipedia.org/wiki/Sinhalese\_language/ [Brahmi2] Wikipaedia on Accessed on 26<sup>th</sup> of May 2009, Brahmi Script: http://en.wikipedia.org/wiki/Br%C4%81hm%C4%AB\_script/

[Code3]Code charts, accessed 29<sup>th</sup> of May 2009, <u>www.unicode.org</u>

[Divehi4] Divehi Akuru, accesed 29<sup>th</sup> of May 2009 http://www.omniglot.com/writing/dhivesakuru.htm

[5]http://www.unicode.org/cldr/data/charts/supplemental/languages\_and\_scripts.html

#### Acknowledgments

This paper would not have been possible without the help of the many. Special thank must go to Bhikkhu Mettha Vihari, for providing some of the documents, which I used for this paper. The help given by Director of Colombo Museum, Dr. Nanda Wickramsinghe who authorized the access to the library of the Museum, and the librarian Ms. Padma Akarawita of the Colombo Museum who tirelessly found three Ola palm leaves with the Sinhala numerals out of the five thousand manuscripts and the assistance rendered by Mr. Senarath Wickremasinghe is specially acknowledged. The author was given special access to Royal Asiatic Society library, the president of the society is specially acknowledged. The president of the Society is especially acknowledged.

The late Prof. VK Samaranayake is remembered for inspiring me to carry out research into Sinhala computerization.

The facilitation rendered by the Information and Communication Technology Agency of Sri Lanka (ICTA), and its Board is hereby acknowledged. Prof. PW Epasinghe and Mr. Reshan Dewapura are remembered for giving recognition to this work officially and encouraging me when I was carrying out the research. Mr. Jayantha Fernando is remembered for his sincere encouragement and believing in my work. Ms. Aruni Goonetilleke is thanked for spending many hours discussion with me finer points on numerals. Dr. Shahani Weerawarana is acknowledged for all the encouragement she gave. The direction given by ICTA's Local Language Working Group (LLWG) and its Chair, Dr. RB Ekanayake is greatly appreciated. Appreciation is given to Mr. Athula Pushpakumara and the ICTA Communications team for the assistance rendered in the publication of this work.

Prof. Gihan Dias and Dr. Ruvan Weerasinghe are gratefully acknowledged for their assistance in the preparation of this paper. Prof. JB Disanayaka is specially acknowledged for sharing his insight into Sinhala Numerals. Heartfelt thanks are given to the late Mr. Rohan N. Wijeratne for his invaluable comments which convinced me that the original report had to be re-drafted.

Prof. KD Paranavithana is acknowledged for his invaluable assistance and participation in the project. Special thanks to Prof. Nimal Silva, Director, Postgraduate Institute of Archaeology, for sharing his thoughts on the subject with me. Acknowledgement is also given to late Prof. Abaya Aryasinghe, who provided us information on the basic concepts of Sinhala numerals, during the very early stages of the research. Special acknowledgement is given to the librarian of the University of Kelaniya for their help in providing reference material.

I also acknowledge my staff at the Software Development Unit of the University of Colombo School of Computing who provided immense help in the preparation of this paper; especially Mr. Ashant Hannan, Senior Software Engineer and Mr. Samira Kodithuwakku, Software Engineer, who accompanied me to numerous organizations in search of documents with numerals.

This work would not have been possible without the assistance of my father Dr. G. Wijayawardhana who helped greatly in the initial preparation of the paper. Finally, but not the least, special thanks are given to my wife Shalika, for the patience she evinces during this work.

Harsha Wijayawardhana.

# Numerations in the Sinhala Language

Harsha Wijayawardhana edited by Aruni Goonetilleke

Every one knows that the Arabs and the Romans have their own numerals. Very few know that the Sinhalese also had their own numerals. No one knew that the Sinhalese numerals had a zero, until Harsha Wijayawardhana told us so. He spent months amidst ruins in our lost cities, museums and libraries to prove, beyond doubt, that the Sinhalese had created a zero, an event that marks a crucial turning point in the history of Sinhala mathematics, when even the Romans could not think of a zero.

Harsha's book will make you think, again and again, about a matter that has escaped our concern. It is hoped that this book will be the beginning of a long journey into the world of Sinhala mathematics and Sinhala writing.

#### J.B.Disanayaka

Professor Emeritus, University of Colombo Ambassador of Sri Lanka to Thailand, Cambodia and Laos.



Strategic Communications and Media Unit - ICTA 160/24, Kirimandala Mawatha, Colombo 05, Sri Lanka, TP: + 94 11 2369099 FAX: + 94 11 2369091 email: info@icta.lk web: www.icta.lk

